

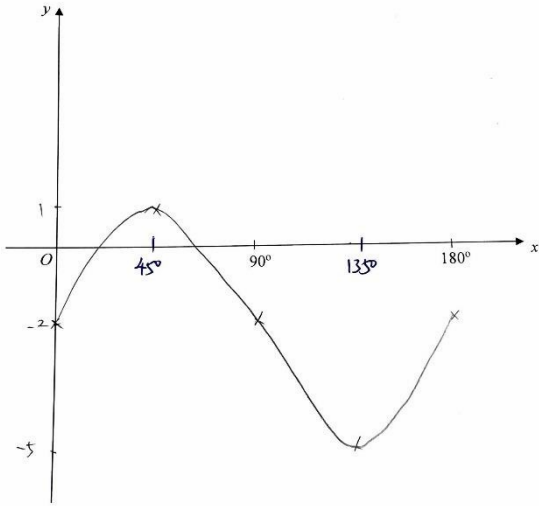
SEMBAWANG SECONDARY SCHOOL
SEC 4NA PRELIMINARY EXAMINATION 2025
ADDITIONAL MATHEMATICS P1 MARKING SCHEME

Qn	Solution
1(i)	$\frac{5\sqrt{7}+2}{3+\sqrt{7}} \times \frac{(3-\sqrt{7})}{(3-\sqrt{7})}$ $= \frac{15\sqrt{7} - (5)(7) + 6 - 2\sqrt{7}}{9-7}$ $= \frac{13\sqrt{7} - 29}{2}$ $= -\frac{29}{2} + \frac{13}{2}\sqrt{7}$
2(a)	$\tan A = \frac{2}{q}$ $\sec A = \frac{1}{\cos A}$ $= \frac{1}{\frac{q}{\sqrt{q^2+4}}}$ $= \frac{\sqrt{q^2+4}}{q}$
2(b)	$\sin 2A = 2 \sin A \cos A$ $= 2 \left(\frac{2}{\sqrt{q^2+4}} \right) \left(\frac{q}{\sqrt{q^2+4}} \right)$ $= \frac{4q}{q^2+4}$

3	$xy = 2 + y^2 \quad \text{---(1)}$ $2y = x - 1 \quad \text{---(2)}$ From (2): $x = 2y + 1 \quad \text{---(3)}$ Sub (3) into (1): $y(2y + 1) = 2 + y^2$ $2y^2 + y - y^2 - 2 = 0$ $y^2 + y - 2 = 0$ $(y + 2)(y - 1) = 0$ $y = -2 \quad \text{or} \quad y = 1$ $x = -3 \quad \text{or} \quad x = 3$
4	$\frac{dV}{dt} = 0.5$ $\frac{dV}{dx} = 2\pi x^2$ When $x = 0.8$, $\frac{dV}{dx} = 2\pi (0.8)^2$ $= 1.28\pi$ $\frac{dV}{dt} = \frac{dV}{dx} \times \frac{dx}{dt}$ $0.5 = 1.28\pi \times \frac{dx}{dt}$ $\frac{dx}{dt} = \frac{0.5}{1.28\pi}$ $\frac{dx}{dt} = \frac{0.5}{1.28\pi}$ $= 0.124 \text{m/h}$
5(a)	$f(3): 2(3)^4 - (3)^3 - 19(3)^2 + 3m + n$ $0 = -36 + 3m + n$ $3m + n = 36 \text{-----} > (1)$ $f(-3): 2(-3)^4 - (-3)^3 - 19(-3)^2 - 3m + n$ $-3m + n = -18 \text{-----} > (2)$ $(1) + (2): 2n = 18$ $n = 9$ $m = 9$

5(a)	By long division method: $f(x) = (x^2 - 9)(2x^2 - x - 1)$ $= (x + 3)(x - 3)(2x + 1)(x - 1)$
6	$\frac{3x-2}{x(x-1)^2} = \frac{A}{x} + \frac{B}{x-1} + \frac{C}{(x-1)^2}$ $3x-2 = A(x-1)^2 + B(x)(x-1) + C(x)$ When $x = 0$, $-2 = A$ When $x = 1$, $C = 1$ When $x = 2$, $B = 2$ $\therefore \frac{3x-2}{x(x-1)^2} = \frac{-2}{x} + \frac{2}{x-1} + \frac{1}{(x-1)^2}$

7	$y = (3 - x^2)\sqrt{2 + x}$ $y = (3 - x^2)(2 + x)^{\frac{1}{2}}$ $\frac{dy}{dx} = (3 - x^2) \frac{1}{2}(2 + x)^{-\frac{1}{2}} + (2 + x)^{\frac{1}{2}}(-2x)$ $\text{When } x = 2, \frac{dy}{dx} = (3 - 2^2) \frac{1}{2}(2 + 2)^{-\frac{1}{2}} + (2 + 2)^{\frac{1}{2}}(-2(2))$ $= -\frac{33}{4}$ $\text{Gradient of normal} = -1 \div -\frac{33}{4}$ $= \frac{4}{33}$ $\text{When } x = 2, y = (3 - 2^2)\sqrt{2 + 2}$ $= -2$ $\text{Sub } x = 2 \text{ and } y = -2 \text{ into } y = \frac{4}{33}x + c$ $-2 = \frac{4}{33}(2) + c$ $c = -\frac{74}{33}$ $\text{Eqn of normal : } y = \frac{4}{33}x - \frac{74}{33}$
8(a)	Amplitude = 3 Period = 180°

8(b)	Correct Shape Amplitude, period x, y intercepts  [3]
9	$\cos 2x + 7 \sin x - 4 = 0$ $1 - 2 \sin^2 x + 7 \sin x - 4 = 0$ $2 \sin^2 x - 7 \sin x + 3 = 0$ $(2 \sin x - 1)(\sin x - 3) = 0$ $\sin x = \frac{1}{2} \text{ or } \sin x = 3 \text{ (rejected)}$ $\text{Basic } \angle = 30^\circ$ $x = 30^\circ, 150^\circ$
10(a)	$f(x) = \int (3x^2 + 4x - 4) dx$ $= \frac{3x^3}{3} + \frac{4x^2}{2} - 4x + c$ $= x^3 + 2x^2 - 4x + c$ $5 = 1 + 2 - 4 + c$ $c = 6$ $f(x) = x^3 + 2x^2 - 4x + 6$

10(b)	$\int_1^2 (x^3 + 2x^2 - 4x + 6) dx$ $= \left[\frac{x^4}{4} + \frac{2}{3}x^3 - 2x^2 + 6x \right]_1^2$ $= \left[\frac{2^4}{4} + \frac{2}{3}(2)^3 - 2(2)^2 + 6(2) \right] - \left[\frac{1}{4} + \frac{2}{3} - 2 + 6 \right]$ $= \frac{101}{12}$
11(a)(i)	$\frac{\pi}{4}$
11(a)(ii)	$-\frac{\pi}{3}$
11(b)	Since principal value of $\cos^{-1} \theta$ is between 0 and π, it is not possible for the principal value of $\cos^{-1} \left(-\frac{\sqrt{2}}{2} \right)$ to be $-\frac{\pi}{4}$. Or principal value of $\cos^{-1} \left(-\frac{\sqrt{2}}{2} \right)$ is $\frac{3\pi}{4}$ so it cannot be $-\frac{\pi}{4}$.
11(c)(i)	$\frac{1}{\sin x + 1} - \frac{1}{\sin x - 1}$ $= \frac{\sin x - 1 - (\sin x + 1)}{(\sin x + 1)(\sin x - 1)}$ $= \frac{-2}{\sin^2 x - 1}$ $= \frac{-2}{1 - \cos^2 x - 1}$ $= \frac{-2}{-\cos^2 x}$ $= 2 \sec^2 x$

11(c)(i)	$\frac{1}{\sin 2x+1} - \frac{1}{\sin 2x-1} = 3$ $2\sec^2 2x = 3$ $\sec^2 2x = \frac{3}{2}$ $\cos^2 2x = \frac{2}{3}$ $\cos 2x = \pm \sqrt{\frac{2}{3}}$ basic angle = 0.615479 $2x = 0.61547, 2.52611, 3.75707, 5.66771$ $x = 0.308, 1.26, 1.88, 2.83 \text{ (to 3s.f.)}$
12(a)	$\frac{d}{dx}(2\sqrt{x}-3)^7$ $= 7(2\sqrt{x}-3)^6 \left(x^{-\frac{1}{2}} \right)$ $= \frac{7(2\sqrt{x}-3)^6}{x^{\frac{1}{2}}} \text{ or } \frac{7(2\sqrt{x}-3)^6}{\sqrt{x}}$
12(b)	$\int_1^4 \frac{7(2\sqrt{x}-3)^6}{x^{\frac{1}{2}}} dx$ $= \left[(2\sqrt{x}-3)^7 \right]_1^4$ $= (2\sqrt{4}-3)^7 - (2-3)^7$ $= 1 - (-1)$ $= 2$ $\int_1^4 \frac{\sqrt{x}(2\sqrt{x}-3)^6}{x} dx = \frac{2}{7}$

13(a)	$y = -x^2 + 2x + 9$ $y = -(x^2 - 2x - 9)$ $y = -[x^2 - 2x + (1)^2 - (1) - 9]$ $y = -[(x-1)^2 - 10]$ $y = -(x-1)^2 + 10$ Maximum value: 10m $x = 1$
13(b)	$-(x-1)^2 + 10 = 0$ $(x-1)^2 = 10$ $x-1 = \pm\sqrt{10}$ $x = 4.16 \text{ m}$ or $x = -2.16$ It takes 4.16m for the stone to reach sea level